

At a seaport, the water has a maximum depth of 15 m at 7:00 a.m. The minimum depth of 5 m occurs 1:30pm. Assume the relation between the depth of the water and time is a sinusoidal function.

a) Write an equation for the depth, h meters, of the water at any time, t hours.

b) Estimate the depth at 11:00 a.m.

c) A cargo ship's hull floats at a depth of 8m. How long can it be in port to load its cargo?

$$h(t) = 5 \cos \left[\frac{2\pi}{13} (t-7) \right] + 10$$

$$y = 8$$

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$$8 = 5 \cos \left[\frac{2\pi}{13} (t-7) \right] + 10$$

$$\frac{-2}{5} = \cos \left[\frac{2\pi}{13} (t-7) \right]$$

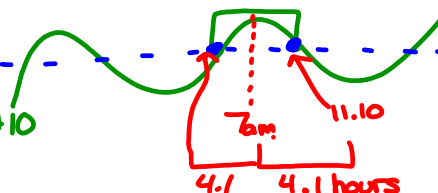
$$\cos^{-1} \frac{-2}{5} = \left[\frac{2\pi}{13} (t-7) \right]$$

$$= 8.2 \text{ hours!}$$

$$\frac{1.98 \cdot 13}{2\pi} = t - 7$$

$$4.101 = t - 7$$

$$t = 11.101$$



An ant gets stuck in your car tire as you drive through a creek 0.3m deep. If your tire is 0.5m tall and rotates once every 0.5sec, how long will the ant have to hold its breath for?

$$y = .25 \cos 4\pi x + .25$$

$$.3 = .25 \cos 4\pi x + .25$$

$$\frac{.05}{.25} = \cos 4\pi x$$

$$\cos^{-1} \frac{.05}{.25} = 4\pi x$$

$$\frac{1.369}{4\pi} = x \quad x \approx 0.109$$

