

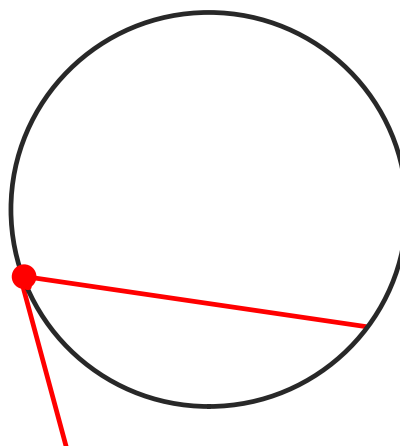
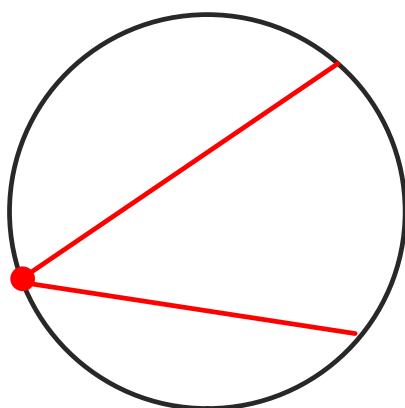
Find the area and perimeter of quadrilateral ABCD

$$\begin{aligned}
 (x+1)^2 + (5x-6)^2 &= (4x+1)^2 \\
 (x^2 + 2x + 1) + (25x^2 - 60x + 36) &= 16x^2 + 8x + 1 \\
 26x^2 - 58x + 37 &= 16x^2 + 8x + 1 \\
 10x^2 - 66x + 36 &= 0 \\
 \frac{10x^2 - 66x + 36}{2} &= 0 \\
 5x^2 - 33x + 18 &= 0 \\
 5x^2 - 3x - 30x + 18 &= 0 \\
 x(5x-3) - 6(5x-3) &= 0 \\
 (x-6)(5x-3) &= 0 \\
 x=6 \quad x=\frac{3}{5} & \\
 \text{extraneous!} & \\
 \text{Per: } 24+24+7+7 &= 62 \\
 \text{Area: } 2 \left(\frac{1}{2} (24)(7) \right) &= 168 \text{ u}^2
 \end{aligned}$$

Angles with vertices ON a circle

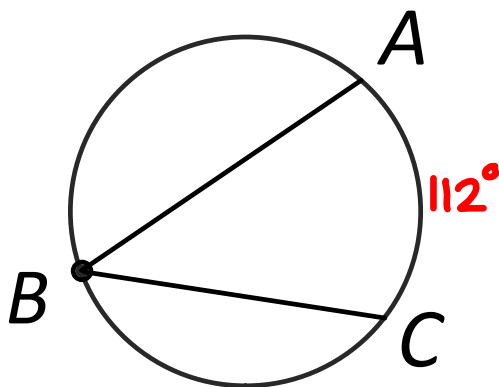
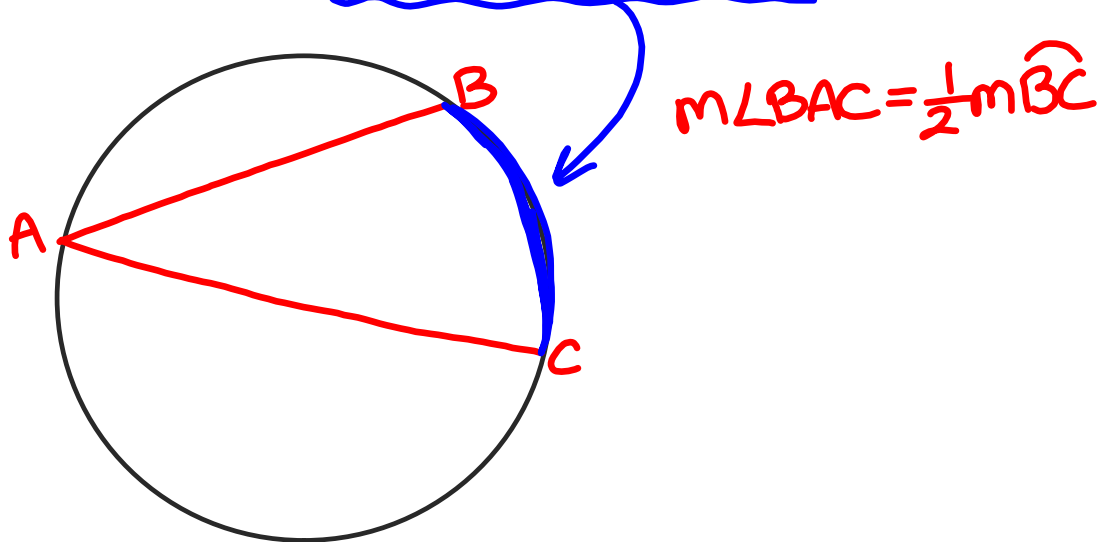
Inscribed Angle

Tangent-Chord Angle



Theorem:

The measure of an angle whose vertex lies on the circle is one-half the measure of its intercepted arc.



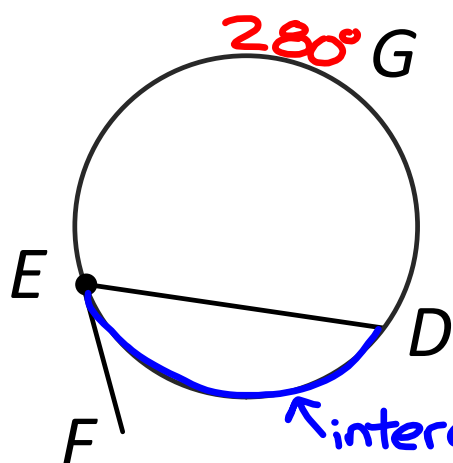
Given: $m\widehat{AC} = 112^\circ$

Find: $m\angle ABC$

$$m\angle ABC = \frac{1}{2}m\widehat{AC}$$

$$m\angle ABC = \frac{1}{2}(112^\circ)$$

$$= 56^\circ$$

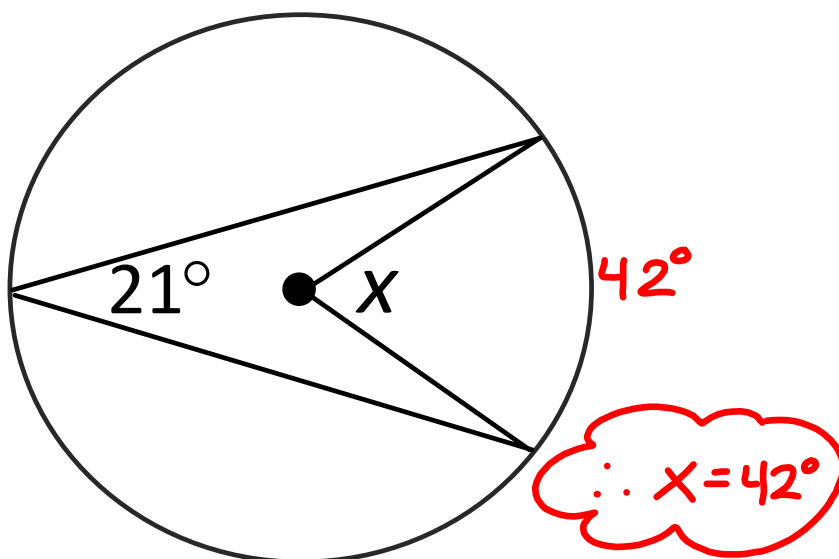


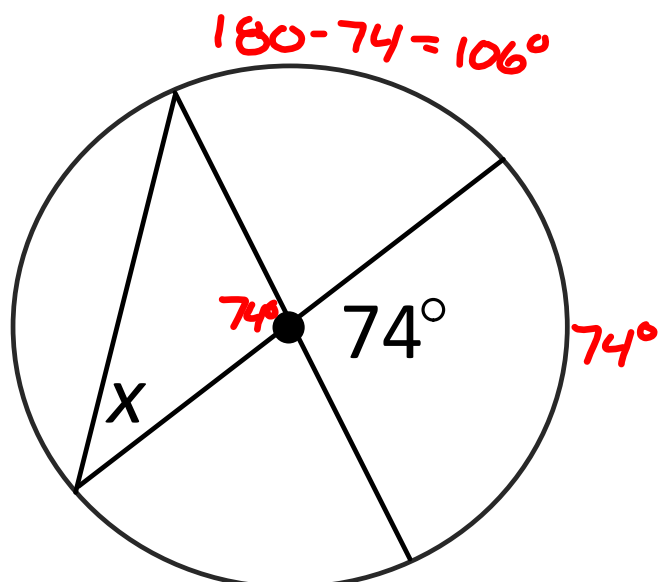
Given: $m\widehat{EGD} = 280^\circ$

Find: $m\angle DEF$

$360^\circ - 280^\circ = 80^\circ$

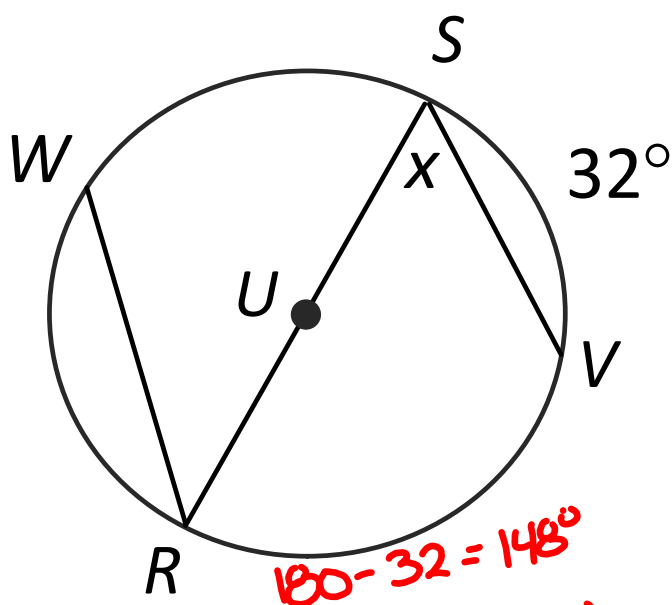
$m\angle DEF = \frac{1}{2}(80^\circ)$
 $= 40^\circ$





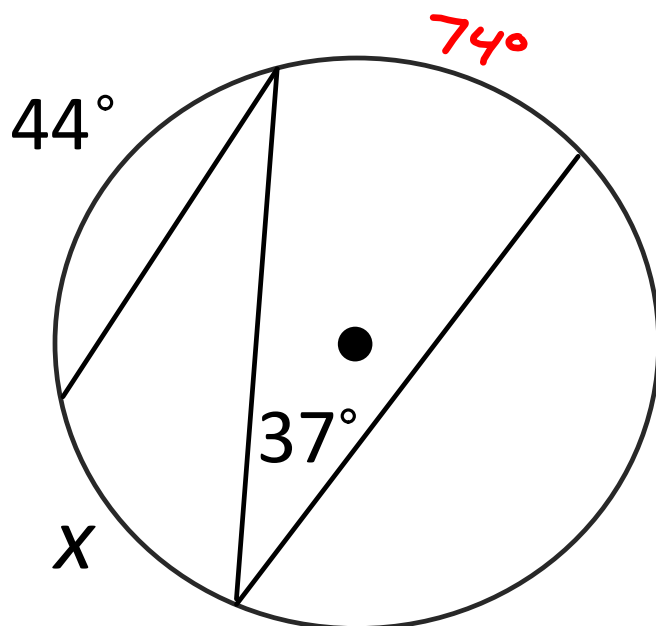
$$X = \frac{1}{2}(106)$$

$$= 53^\circ$$



$$X = \frac{1}{2}(148)$$

$$= 74^\circ$$

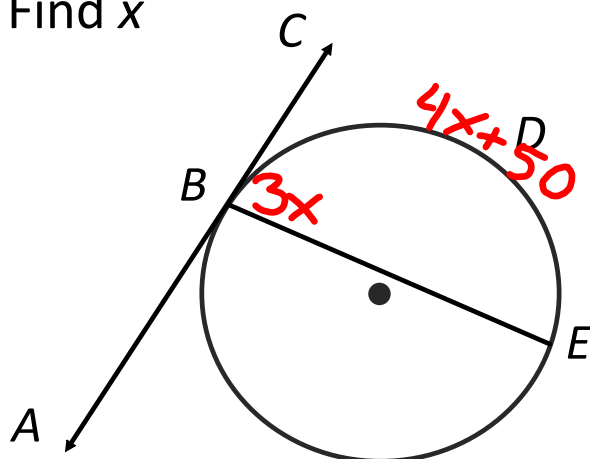


109°

$$360 - 44 - 74 - 109 = x$$

$$133^\circ = x$$

Find x



$$m\angle CBE = 3x$$

$$m\widehat{BDE} = 4x + 50$$

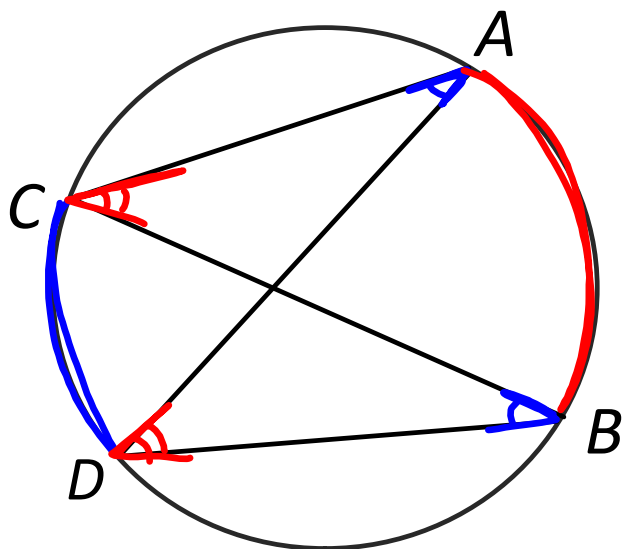
$$3x = \frac{1}{2}(4x + 50)$$

$$3x = 2x + 25$$

$$x = 25$$

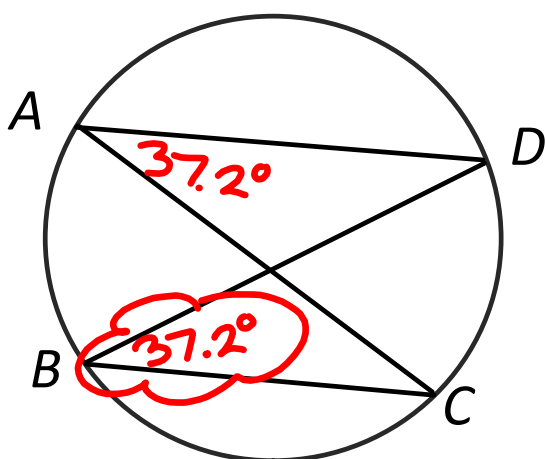
Theorem:

If two inscribed angles of a circle intercept the same arc, then the angles are congruent.



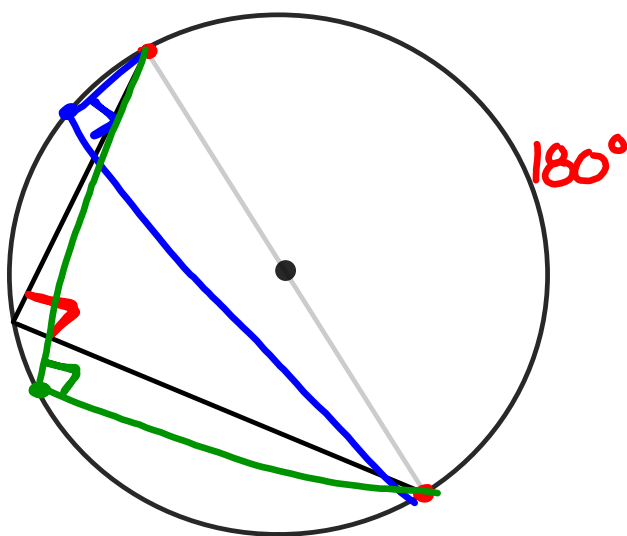
Given: $m\angle DAC = 37.2^\circ$

Find: $m\angle CBD$

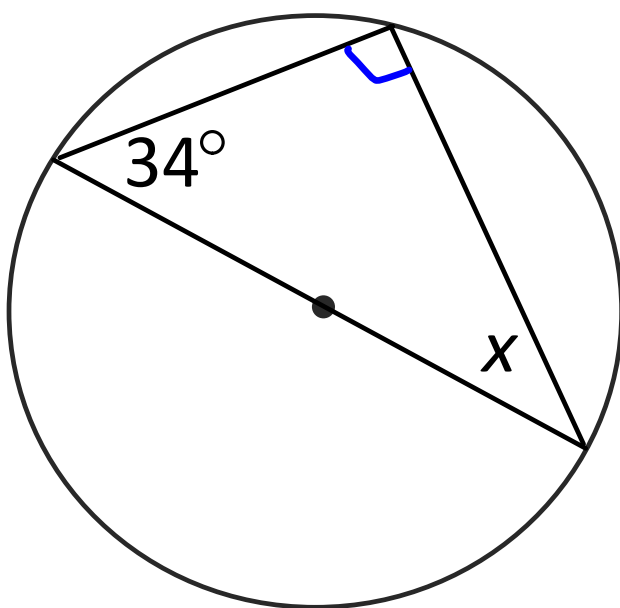


Theorem:

An angle inscribed in a semicircle is a right angle



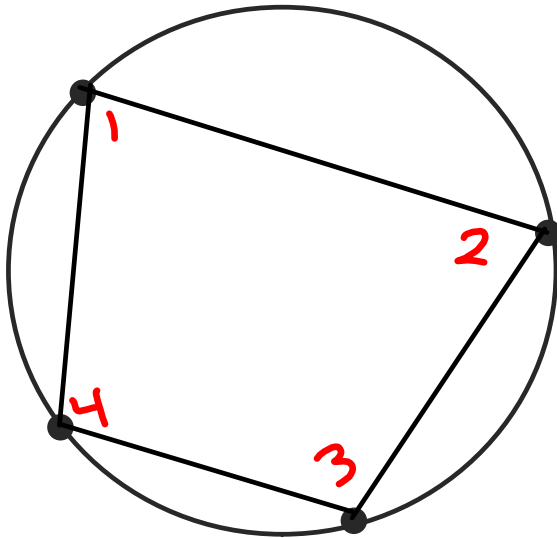
Find x



$$x + 34^\circ = 90$$
$$x = 56^\circ$$

Theorem:

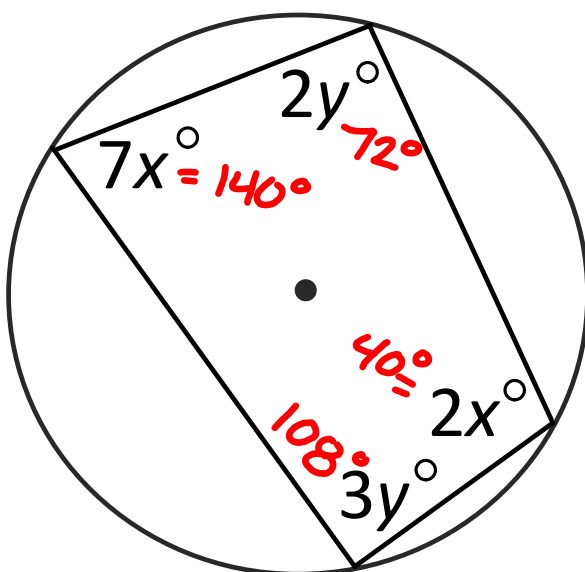
A quadrilateral can be inscribed in a circle iff its opposite angles are supplementary.



$$m\angle 1 + m\angle 3 = 180^\circ$$

$$m\angle 2 + m\angle 4 = 180^\circ$$

Find the measure of each interior angle of the quadrilateral



$$2x + 7x = 180^\circ$$

$$9x = 180$$

$$x = 20$$

$$2y + 3y = 180$$

$$5y = 180$$

$$y = 36$$