

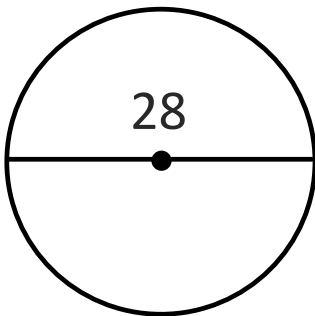
## Warm-up

On Handout

The **CIRCUMFERENCE** of a circle is the distance around it (perimeter)

$$C = \pi d \quad \text{OR} \quad C = 2\pi r$$

Circumference = ?

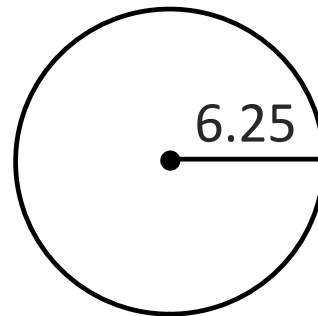


$$C = d\pi$$

$$C = 28\pi \text{ exact!}$$

$$C \approx 87.965 \text{ approx}$$

Circumference = ?



$$C = 2\pi r$$

$$C = 2\pi(6.25)$$

$$= 12.5\pi$$

Find the indicated measure

- a) Circumference of a circle with a radius of 23 ft

$$C = 46\pi \text{ ft}$$

- b) Diameter of a circle with a circumference of 64 meters

$$C = d\pi$$

$$64 = d\pi$$

$$d = \frac{64}{\pi} \text{ m}$$

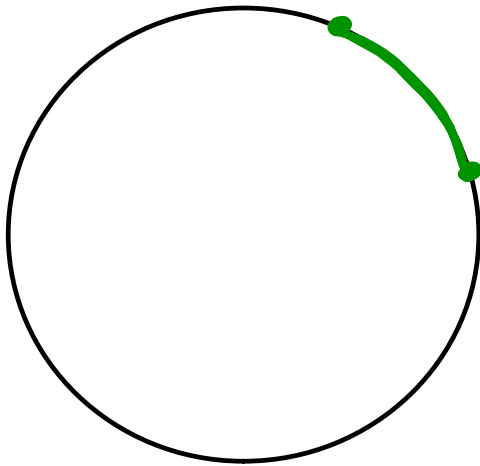
- c) Radius of a circle with a circumference of 58 centimeters

$$C = 2\pi r$$

$$58 = 2\pi r$$

$$r = \frac{58}{2\pi} = \frac{29}{\pi} \text{ cm}$$

Def'n: An **ARC** of a circle is made up of two points on the circle and all points on the circle needed to connect them by a single path



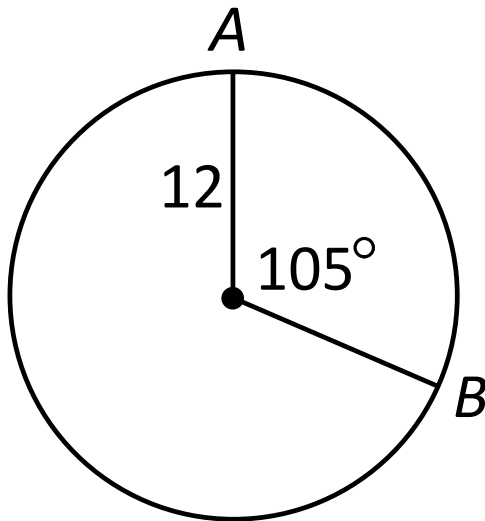
# of degrees of circle that arc contains: *arc measure*

if flattened the arc and used a ruler: *arc length*

Formula for Arc Length:

$$\frac{\text{Arc Length}}{\text{Circumference}} = \frac{m \overset{\frown}}{360^\circ}$$

Find the length of  $\widehat{AB}$



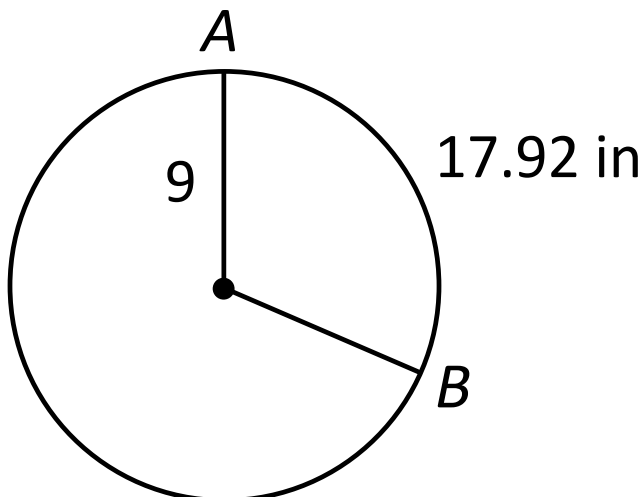
$$\frac{x}{2\pi r} = \frac{105^\circ}{360^\circ}$$

$$\frac{x}{24\pi} = \frac{7}{24}$$

$$\frac{24x}{24} = \frac{7 \cdot 24 \cdot \pi}{24}$$

$$\boxed{x = 7\pi} \checkmark$$

Find  $m\widehat{AB}$



$$\frac{17.92}{18\pi} = \frac{x}{360^\circ}$$

$$x \cdot 18\pi = 6451.2$$

$$x = \frac{6451.2}{18\pi}$$

$$\boxed{x = \frac{358.4^\circ}{\pi}}$$

Find the circumference of a circle if the arc intercepted by a  $112^\circ$  central angle has a length of 37 cm

$$\frac{37}{C} = \frac{112^\circ}{360^\circ}$$

$$\frac{37}{C} = \frac{14}{45}$$

$$14C = 1665$$

$$C = \frac{1665}{14} \text{ cm}$$

Find the radius of a circle if a minor arc has a measure of  $45^\circ$  and a length of 20 ft

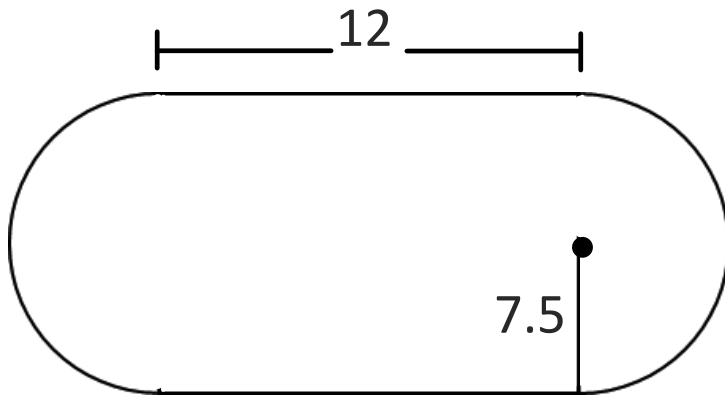
$$\frac{20}{2\pi r} = \frac{45^\circ}{360^\circ}$$

$$\frac{10}{\pi r} = \frac{1}{8}$$

$$\pi r = 80$$

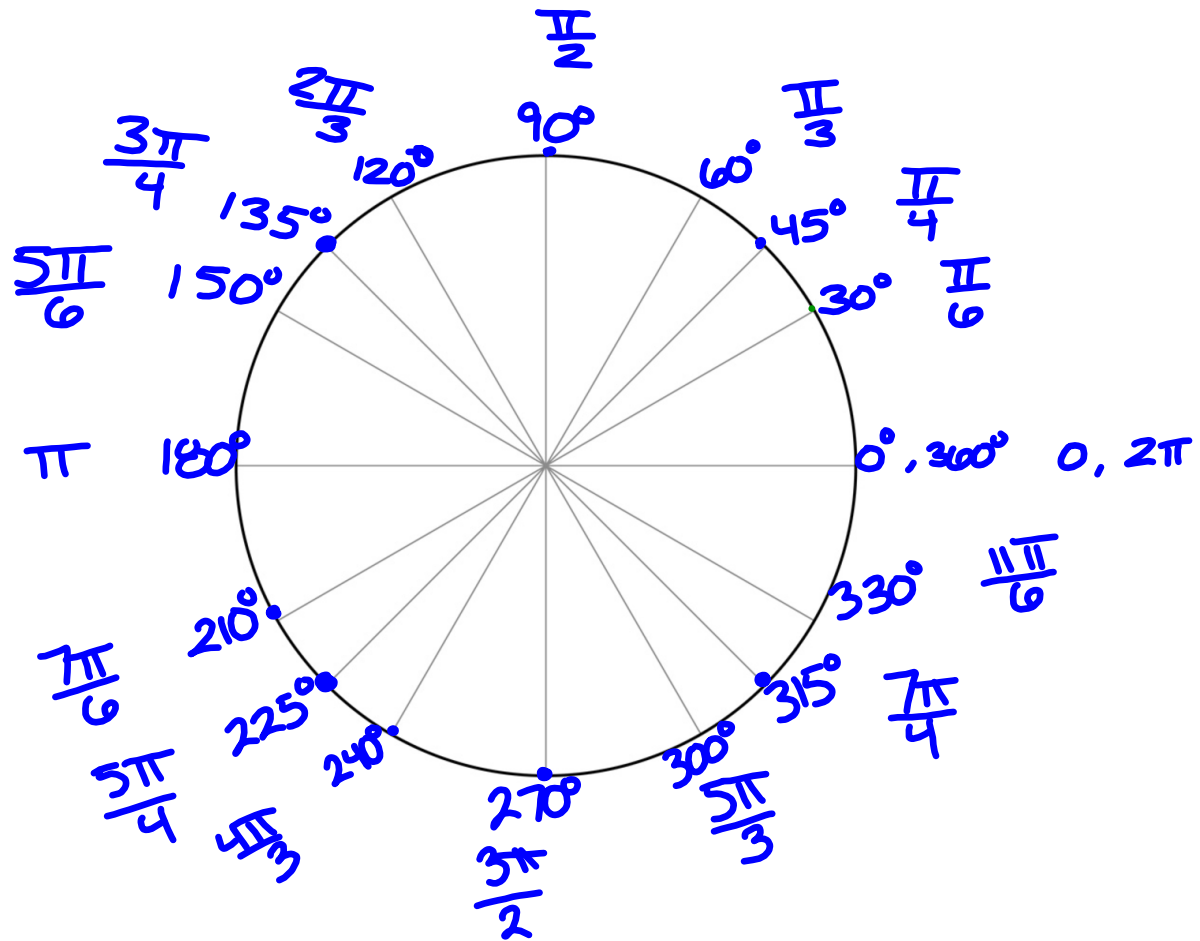
$$r = \frac{80}{\pi} \text{ ft}$$

Find the perimeter of the figure



$$\begin{aligned} P &= 12 + 12 + 2\pi(7.5) \\ &= 24 + 15\pi \text{ units} \end{aligned}$$

A RADIANT is defined as the measure of a central angle that occurs when one radius of a circle is "wrapped around" the circumference of the circle.



Converting from DEGREES to RADIANS

$$\text{rad} = \text{deg} \left( \frac{\pi}{180^\circ} \right)$$

Converting from RADIANS to DEGREES

$$\text{deg} = \text{rad} \left( \frac{180^\circ}{\pi} \right)$$

Convert to the other form:

$$\text{a) } 75^\circ \cdot \frac{\pi}{180^\circ} = \frac{5\pi}{12}$$

$$\text{b) } -36^\circ \cdot \frac{\pi}{180^\circ} = -\frac{\pi}{5}$$

$$\text{c) } \frac{2\cancel{\pi}}{9} \cdot \frac{180^\circ}{\cancel{\pi}} = 40^\circ$$

$$\text{d) } -\frac{5\cancel{\pi}}{6} \cdot \frac{180^\circ}{\cancel{\pi}} = -150^\circ$$